

MF22 Equation Sheet

Calculating the thermodynamics of fuel cells

$$\Delta G = -nFE_{OC}$$

Nernst Equation

$$E_{OC} = E_{OC}^{\circ} - \frac{nF}{RT} \ln \left(\frac{[products]}{[reactants]} \right)$$

$$\text{for fuel cell} \quad \left(\frac{[products]}{[reactants]} \right) = \left(\frac{[H_2O]}{[H_2]\sqrt{[O_2]}} \right)$$

Temperature dependence of E_{OC}

$$E_{OC} = E_{OC}^{\circ} + \frac{\Delta S}{nF} (T - T^{\circ})$$

Butler-Volmer Kinetics

$$i = i_o \left([O_2]^* e^{\frac{\alpha F}{RT} \eta} - [H_2O]^* e^{-\frac{(1-\alpha)F}{RT} \eta} \right)$$

Potential Losses

$$E_{loss} = \eta^a + \eta^c + jR_{mt} \quad E_{cell} = E_{OC} - E_{loss}$$

Activation Polarisation

$$\Delta V_{act} = \eta = E - E_{EQM} = \frac{RT}{\alpha F} \ln \left(\frac{i}{i_o} \right)$$

Concentration Polarisation

$$\Delta V_c = E - E_{EQM} = \frac{RT}{nF} \ln \left(\frac{[C^*]}{[C_o]} \right)$$

Ohmic Resistive Losses

$$V_{Ohm} = i \times R_{total}$$

Fuel Cell Efficiency

$$\xi = \Delta H \frac{V}{nF} = \frac{V}{1.482} \text{ for hydrogen}$$

Linear Approximation of IV Curves

$$i = \frac{V_{OC} - V_{cell}}{k}$$

$$W = V_{cell} \times i$$

$$W_{max} = \frac{V_{OC}^2}{4k} \text{ and is reached when } V_{cell, W_{max}} = \frac{V_{OC}}{2}$$

Stoichiometry Factor

$$\lambda = \frac{nFNHw}{I}$$

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Efficiency of Thermoelectric Devices

$$ZT = \frac{S^2 \sigma T}{\kappa}$$

Kinetic of Nucleation

$$\Delta G = 4\pi r^2 \gamma + \frac{4}{3} \pi r^3 \Delta g_v$$

$$r_c = -\frac{2\gamma}{\Delta g_v}$$

$$\Delta G_c = \frac{16\pi\gamma^3}{3(\Delta g_v)^2}$$

Nucleation Rate

$$k_n = A e^{-\left(\frac{\Delta G_c}{kT}\right)}$$

Gibbs-Thomson Relationship

$$\ln S = \frac{2\gamma v}{kTr}$$

DVLO Theory (Attractive Van der Waals and Electrical Repulsion)

$$V_A = \frac{Aa}{12} H$$

$$V_R = \varepsilon a \psi_0^2 \ln(1 + e^{-\kappa H})$$

$$\kappa^{-1} = \sqrt{\frac{\varepsilon_0 \varepsilon_r kT}{2N_A e^2 I}}$$

Brus Equation

$$E_{QD} = E_B + \frac{\pi^2 \hbar}{2R^2} \left(\frac{1}{m_e^*} + \frac{1}{m_h^*} \right)$$

Dynamic Light Scattering

$$D = \frac{kT}{6\pi\alpha\eta}$$

X-Ray Photoelectron Spectroscopy

$$KE = h\nu - BE - \phi$$

$$BE_F = h\nu - KE - \phi_{spec}$$

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Optical Resolution

$$D = \frac{\lambda}{2\sin\theta}$$

Probe Sample Convolution

$$L = \sqrt{4Rr}$$

Bell Evans Model

$$\langle f^* \rangle = \frac{k_b T}{x_t} \ln \left(\frac{r x_t}{k_{off} k_b T} \right)$$

Friddle-Noy Model

$$\langle f^* \rangle = f_{eq} + \frac{k_b T}{x_t} \ln \left(1 + e^{-g} \frac{r x_t}{k_{u(f)} k_b T} \right)$$

FRET

$$\phi_f = \frac{\textit{photons emitted}}{\textit{photons absorbed}}$$

$$I = I_0 e^{-\left(\frac{t}{\tau}\right)}$$